



Distributed Probabilistic Forecasting For New Energy Systems Operation

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- ❖ Strategic role of **information** in new energy systems (reserve activation, flexibility management, multicommodity energy trading) -> need for new efficient **forecasting methods**.
- ❖ Multimodal dataset with **massive, heterogenous** and **geographically spread** data sources.

Goal: forecast weekly solar PV power production using multimodal data sources / features and forecasting methods.

A) set of experts

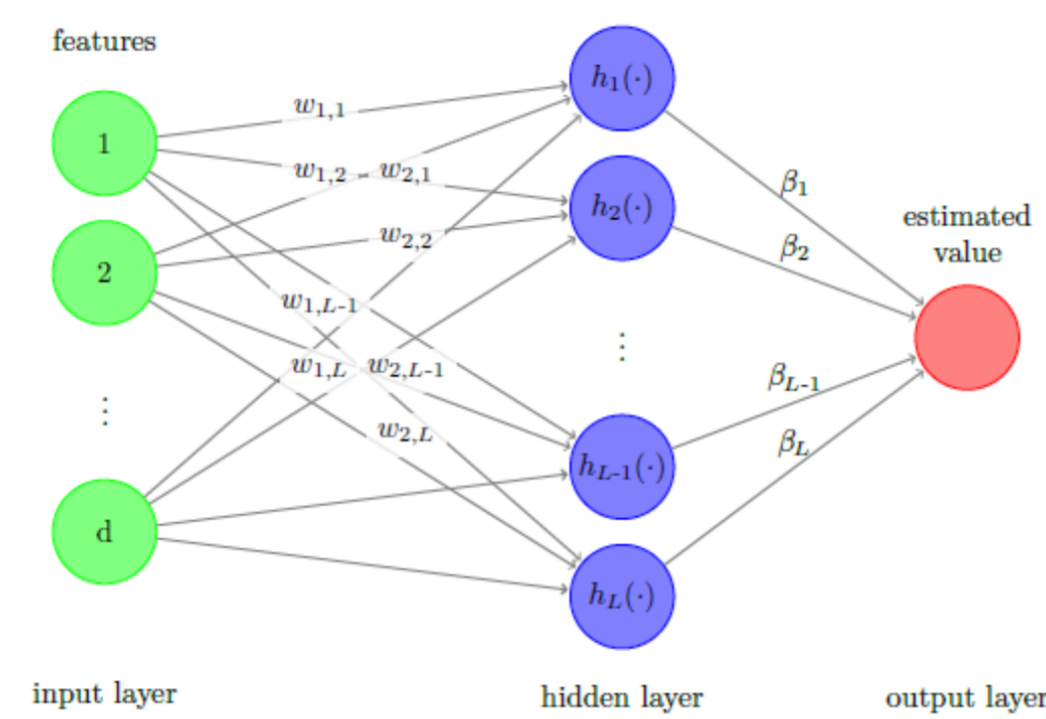
A) Prediction Interval (PI) based ELM

Single hidden layer feed-forward Neural Network
Random selection of input weights and thresholds

Output weights determined through matrix computation

$$f_L(\mathbf{x}) = \sum_{j=1}^L \beta_j h_j(\mathbf{x}) = \mathbf{h}(\mathbf{x})\boldsymbol{\beta}, \forall \mathbf{x} \in \mathbb{R}^d$$

$$\hat{\boldsymbol{\beta}} = \mathbf{H}^+ \mathbf{T} \quad \text{with } \mathbf{H} = \begin{pmatrix} h_1(\mathbf{x}_1) \\ \vdots \\ h_L(\mathbf{x}_{n_{\text{train}}}) \end{pmatrix}$$



Training data corrupted by noise

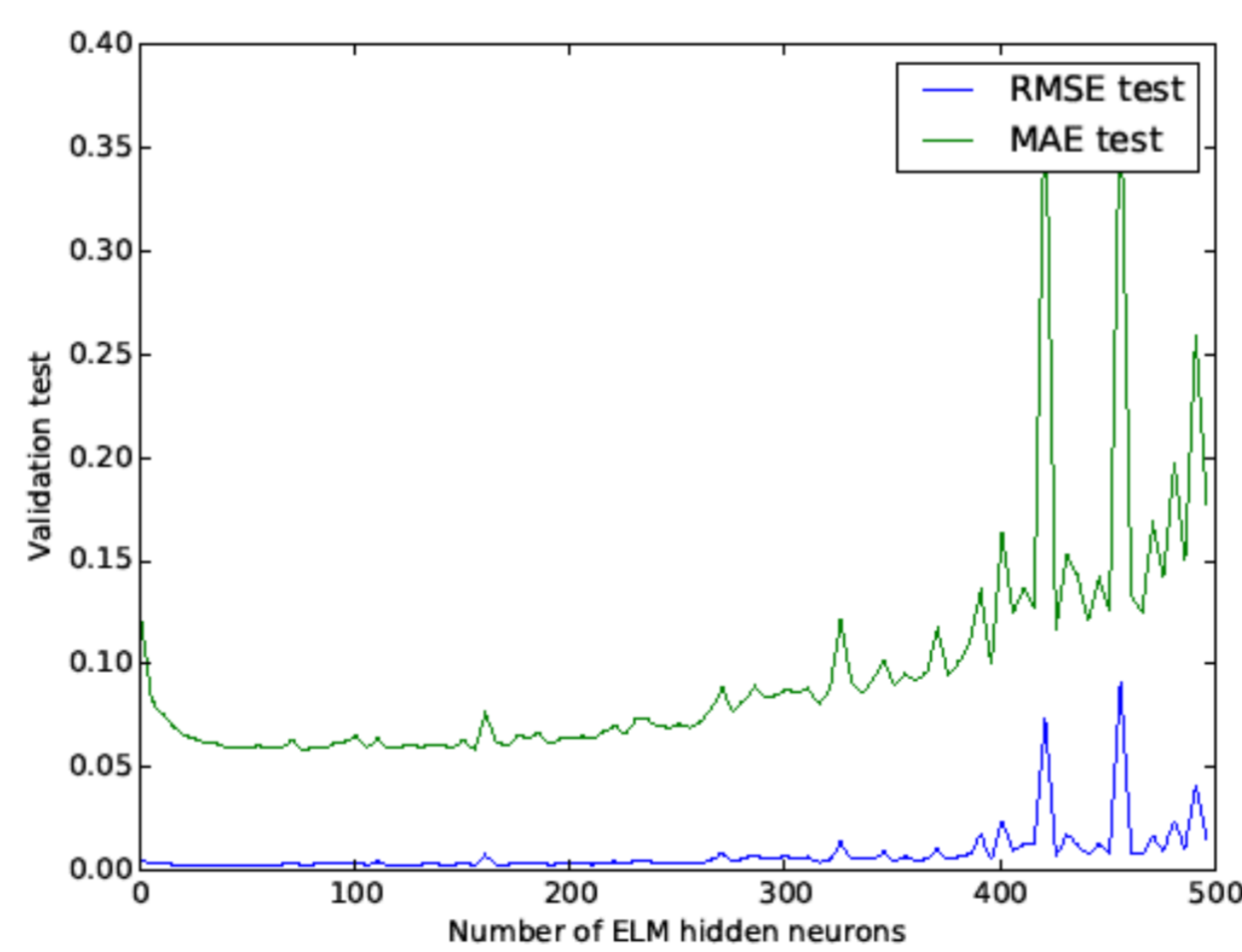
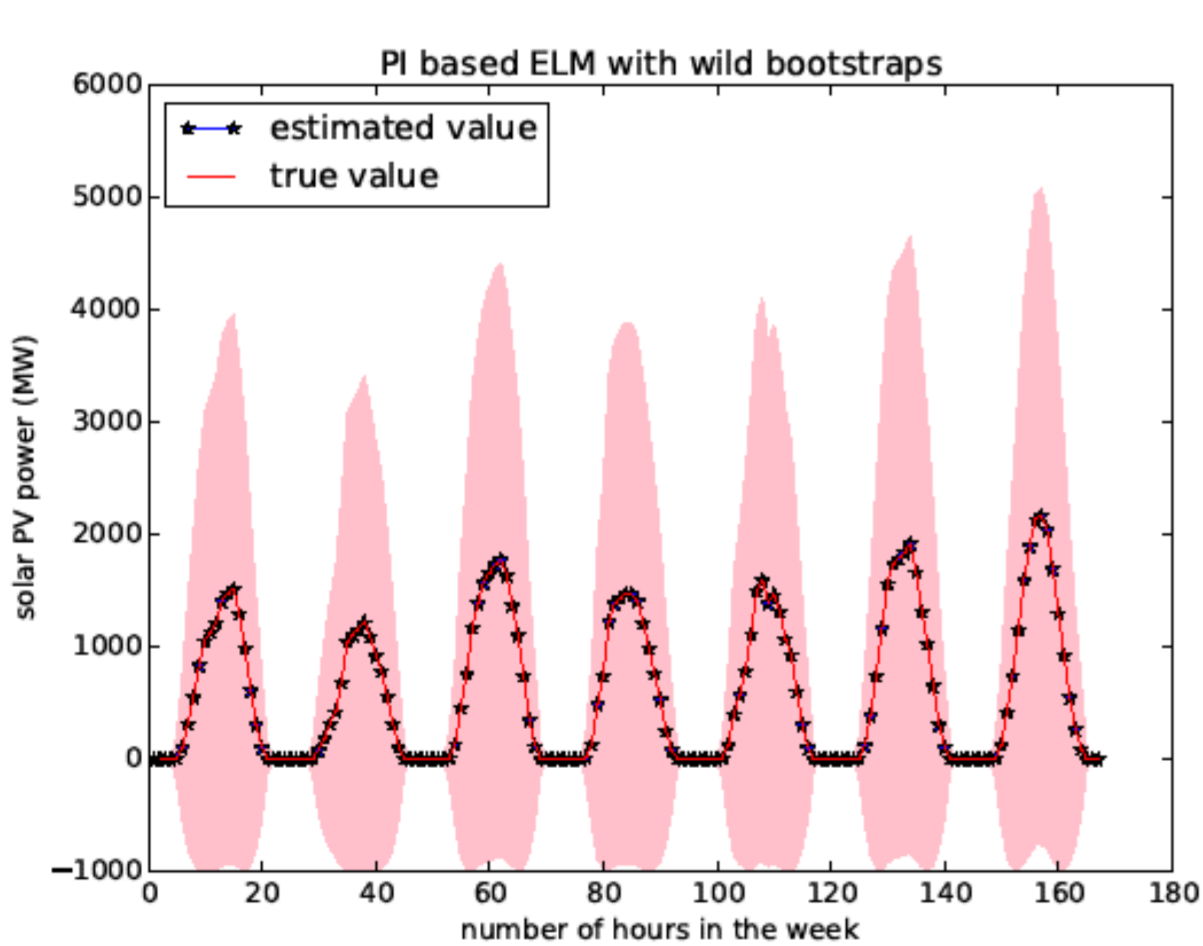
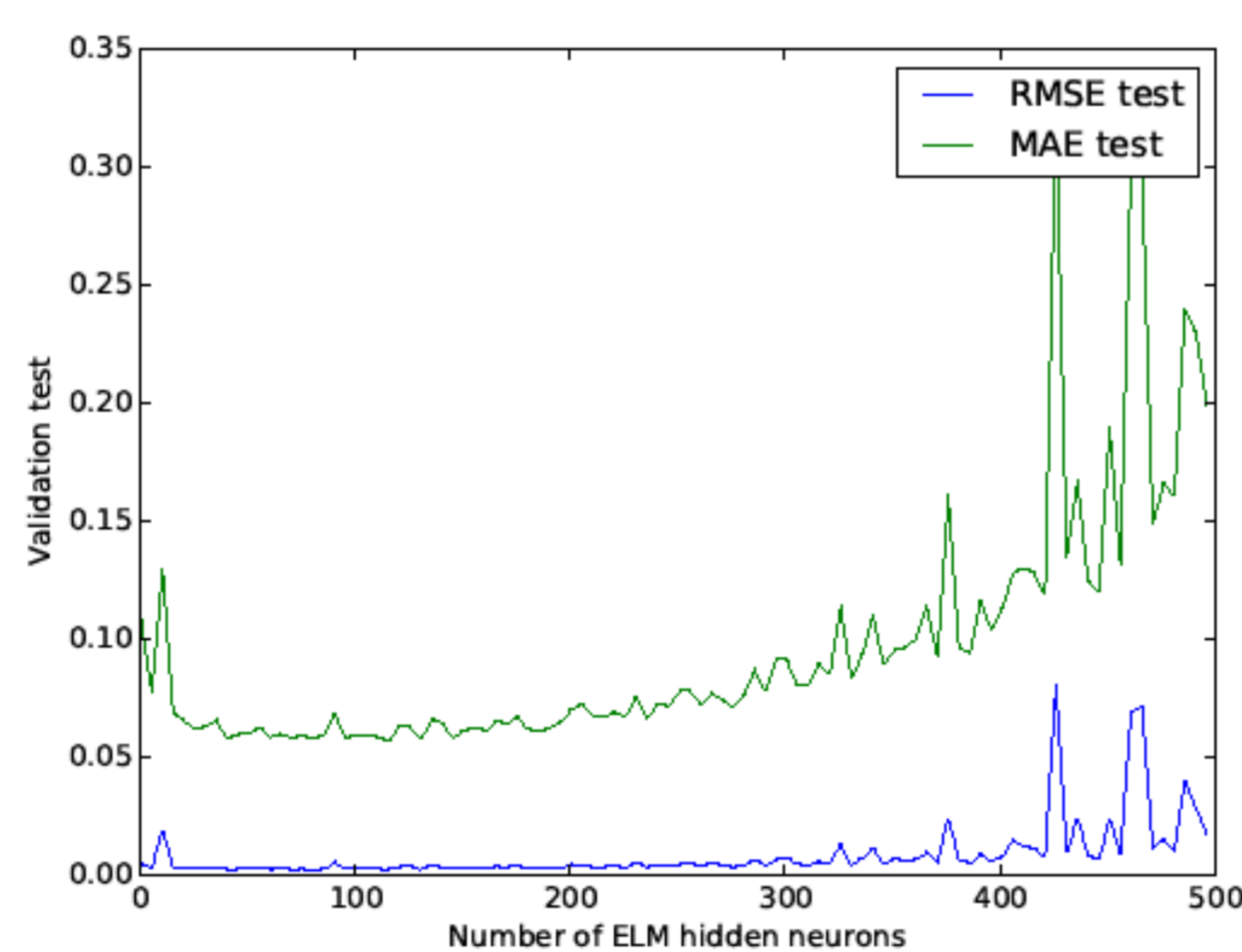
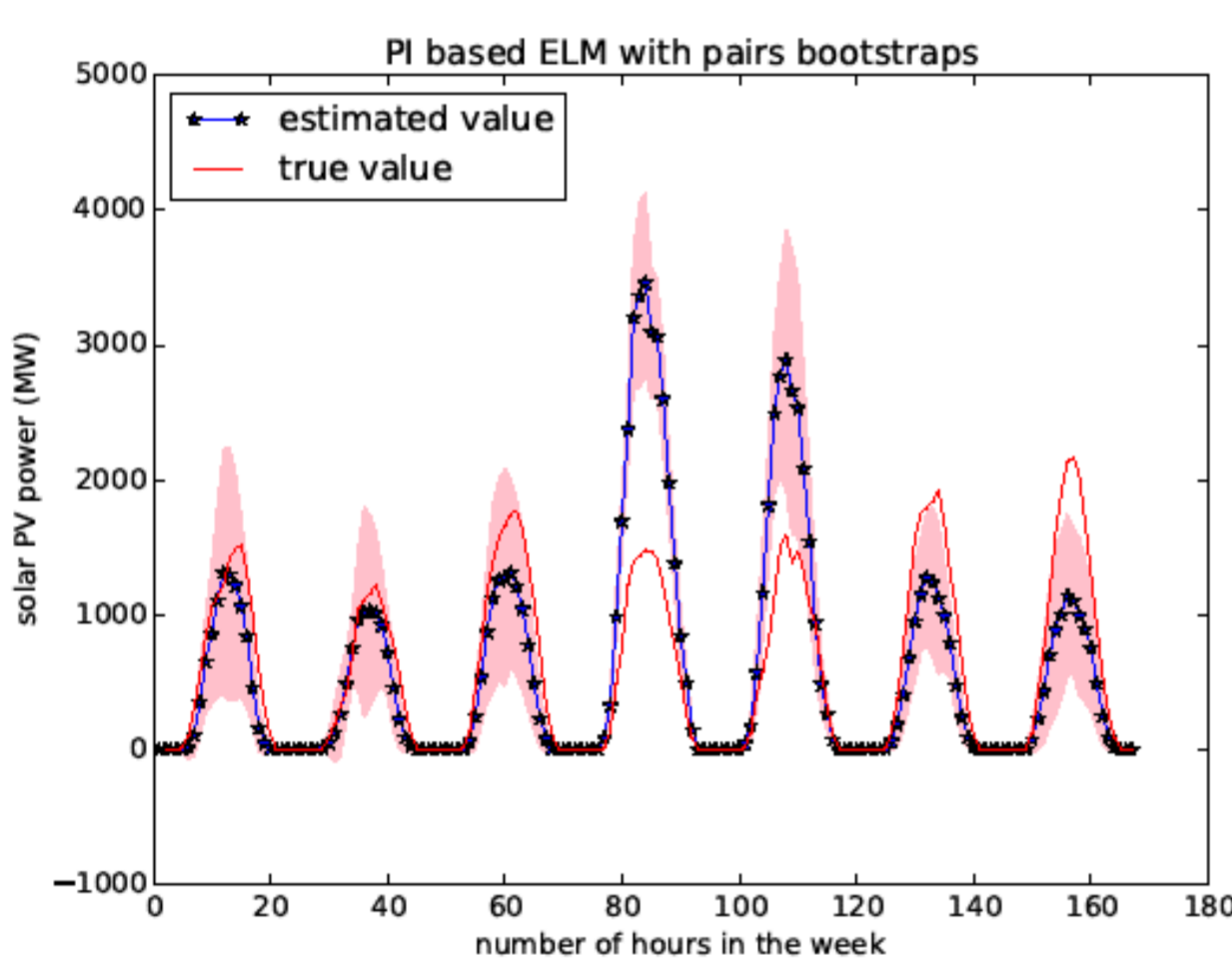
$$t_i = f_L(\mathbf{x}_i) + \epsilon(\mathbf{x}_i)$$

$\alpha \in [0; 1]$ confidence level of the PI defined by its bounds

$$L_\alpha(\mathbf{x}_i) := \hat{y}(\mathbf{x}_i) - z_{1-\frac{\alpha}{2}} \sqrt{\sigma_i^2(\mathbf{x}_i)}$$

$$U_\alpha(\mathbf{x}_i) := \hat{y}(\mathbf{x}_i) + z_{1-\frac{\alpha}{2}} \sqrt{\sigma_i^2(\mathbf{x}_i)}$$

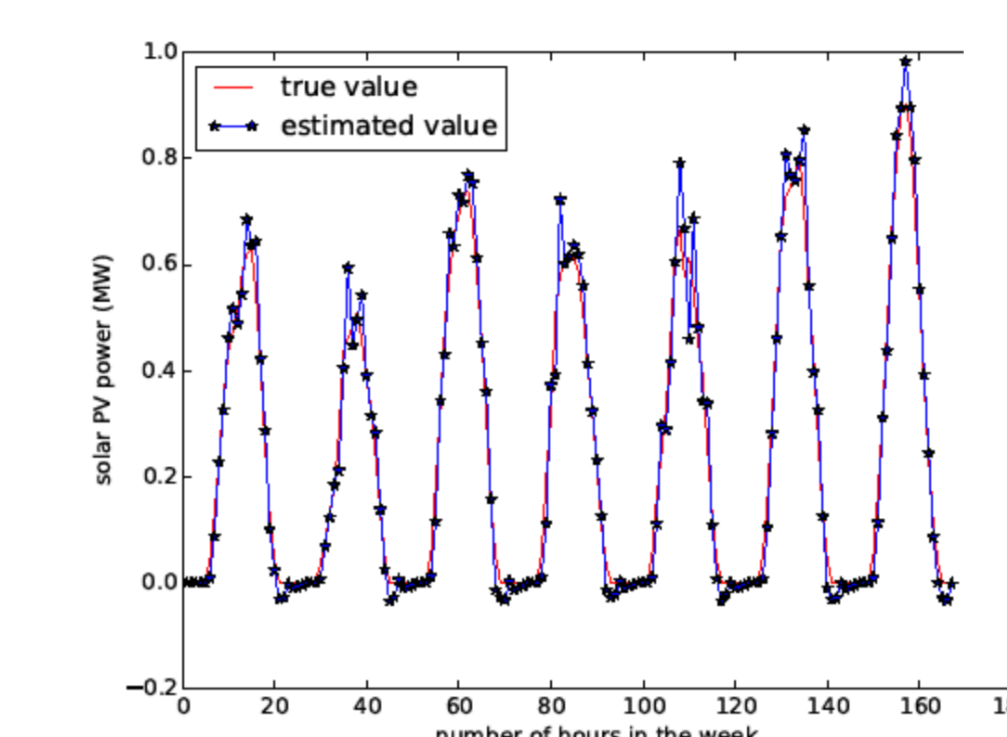
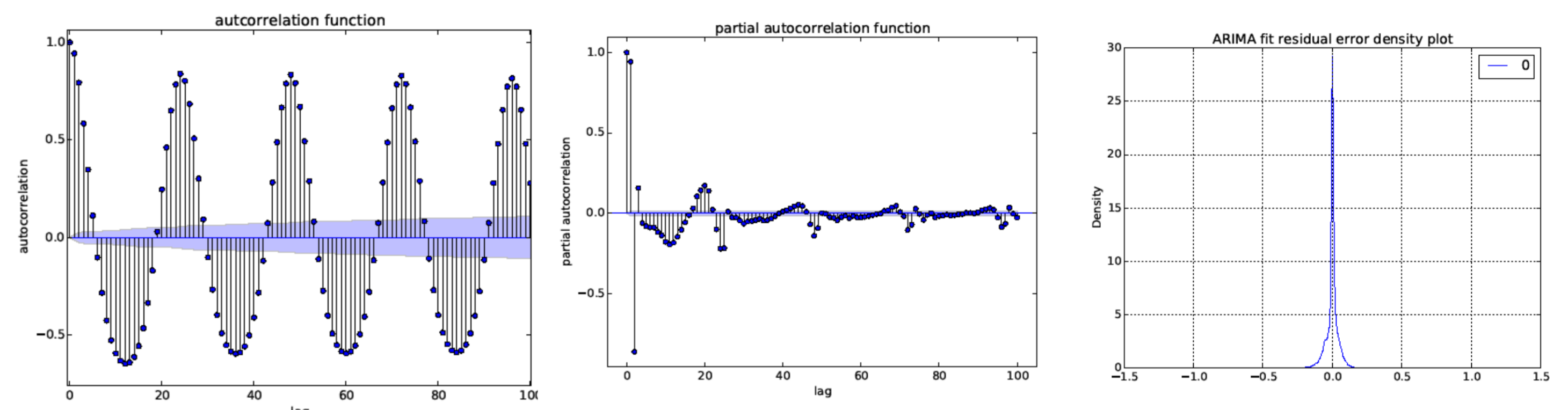
Computed via **bootstrap techniques**. For $\alpha=90\%$ pairs / wild bootstrap and cross-validation



performance \ bootstrap	pairs	wild	resampling
PICP	0.601	1.0	1.0
Score	0.187	0.953	0.953
MAE (MW)	-0.088	$4.785 \cdot 10^{-15}$	$5.800 \cdot 10^{-15}$
Mean absolute error (MW)	0.095	$4.602 \cdot 10^{-14}$	$4.501 \cdot 10^{-14}$
RMSE (MW)	0.012	$7.254 \cdot 10^{-15}$	$7.206 \cdot 10^{-15}$

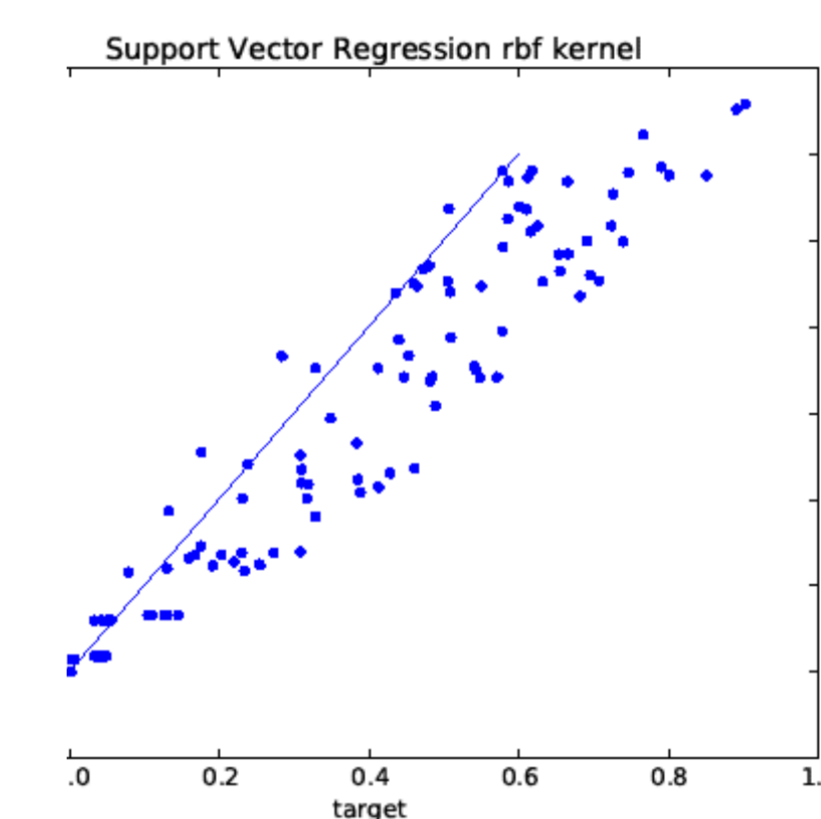
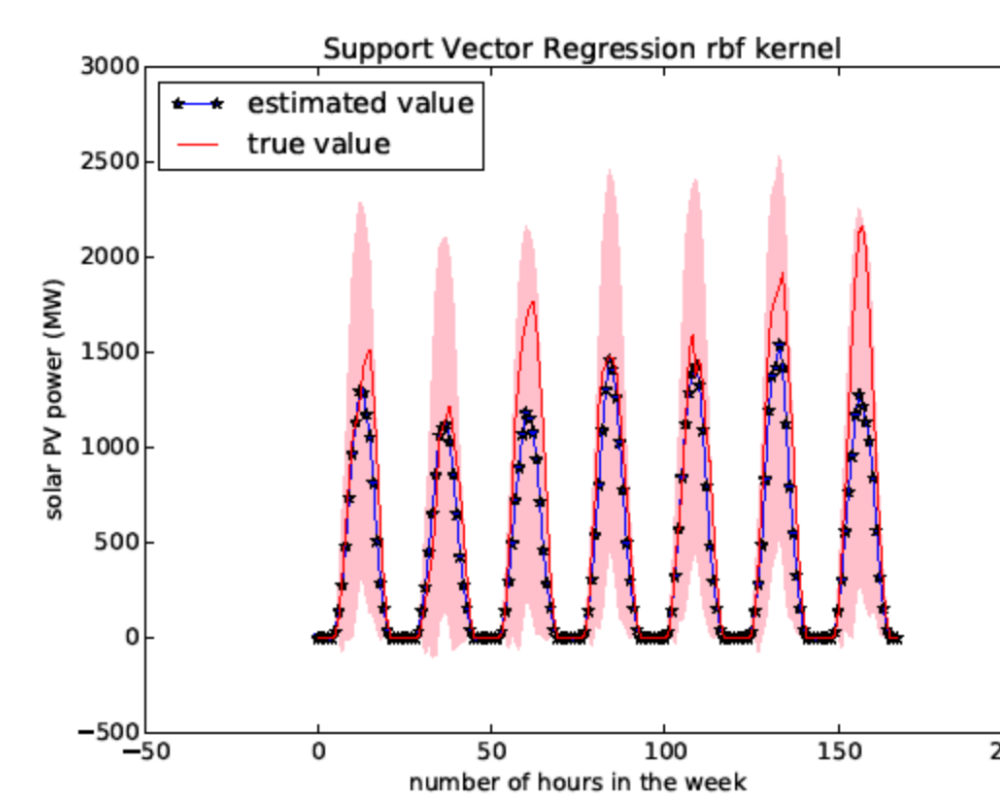
B) Rolling forecast ARIMA

Stationarization of the time series by removing moving average and trend. ARIMA model fitted based on ACF and PACF plots



performance	rolling ARIMA
MAE (MW)	-0.021
Mean absolute error (MW)	51.010
RMSE (MW)	0.394

C) SVR forecast



performance \ kernel	RBF
MAE	-5.908
Mean Absolute Error	5.908
RMSE	2.274

Feature / Expert selection

A set of meteorological stations spread over a region.

Goal is to **forecast regional solar PV power**.

Each station is associated with an **expert**.

Station observations are **historical regional**

PV power and **meteorological features**.

Automatic feature selection based on **mRMR** criterion derived from Mutual Information of $x \sim p_X(x)$ and $y \sim p_Y(y)$ two features

$$I(x, y) := \iint p_{X,Y}(x, y) \log \frac{p_{X,Y}(x, y)}{p_X(x)p_Y(y)} dx dy$$

Experts activated based on the **randomized EWA forecaster**.

Features	PICP	Score	Nb of Experts	Experts Index	mRMR
Wind Speed	0.904	0.093	8/13	4, 6, 12, 1, 11, 8, 3, 9	800
Wind Dir.	0.889	0.095	8/13	4, 12, 6, 1, 8, 11, 3, 9	780
Cloud Cover	0.910	0.094	8/13	4, 12, 6, 1, 11, 8, 3, 9	2.10^3
Precipitation	0.916	0.098	8/13	4, 6, 1, 12, 11, 8, 3, 9	5.10^3
Temperature	0.907	0.098	8/13	4, 12, 6, 1, 11, 8, 3, 9	10^3
Pressure	0.875	0.090	8/13	4, 6, 12, 1, 11, 8, 3, 9	100
Sun Zenith	0.886	0.091	8/13	4, 6, 12, 1, 8, 11, 3, 9	80
Sun Azimuth	0.913	0.097	8/13	4, 12, 6, 1, 8, 11, 3, 9	3.10^3

Derivation of a **convergence bound** on the expected regret for the group of activated experts.